

Cardinal Numbers of Some Sets (VIII)*.

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Let X be an infinite set, $C = \{B: B \text{ is a Boolean algebra defined on the } X\}$, Define $\bar{B} = \{D: D \text{ is isomorphic to } B\}$, $C_1 = \{\bar{B}: B \in C \text{ \& } B \text{ is atomic}\}$, $C_2 = \{\bar{B}: B \in C \text{ \& } B \text{ is not atomic}\}$, then $|C_1| = |C_2| = 2^{|X|}$. The power set of X is denoted by $P(X)$, $P(X)$ is a field of sets (Under Union and Intersection of sets, and Complement of set), Suppose $K = \{F: F \text{ is a field of sets \& } F \subseteq P(X)\}$, $K_1 = \{\hat{F}: F \in K\}$, $K_2 = \{\hat{F}: F \in K \text{ \& } F \text{ is not atomic}\}$ then $|K_1| = |K_2| = 2^{2^{|X|}}$.



Cardinal Numbers of Some Sets (IX)*

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Let X be an infinite set, $C = \{G: G \text{ is a group defined on the } X\}$, Define $\hat{G} = \{H: H \text{ is isomorphic to } G\}$, $C_2 = \{\hat{G}: G \in C \text{ \& } G \text{ is not commutative}\}$, then $|C_2| = 2^{|X|}$. If $K = \{F: F \text{ is a division ring defined on the } X\}$, $K_1 = \{\hat{F}: F \in K \text{ \& } F \text{ is not commutative}\}$, $K_2 = \{\hat{F}: F \in K \text{ \& } F \text{ is commutative}\}$, then $|K_1| = |K_2| = 2^{|X|}$. Suppose $T(X) = \{\varphi: \varphi \in X^X \text{ \& } \varphi \text{ is bijective}\}$, $S = \{G: G \text{ is a subgroup of } T(X)\}$, $S_1 = \{\hat{G}: G \in S \text{ \& } G \text{ is commutative}\}$, $S_2 = \{\hat{G}: G \in S \text{ \& } G \text{ is not commutative}\}$, then $|S_1| = |S_2| = 2^{2^{|X|}}$.
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